

① ~~gwnotes~~

Saaghal.net/pages/uhwsno  
.html

② Binaries

GWs from a Strong PBH PT

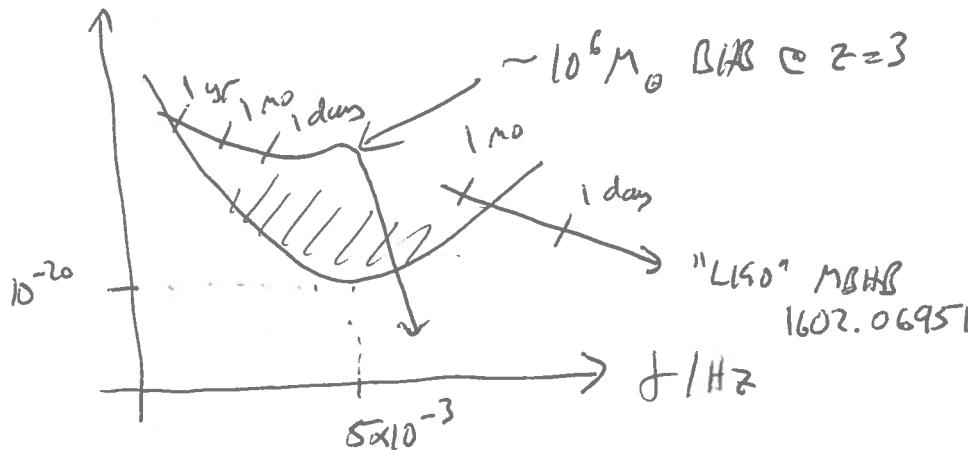
LISA (1702.00786 + Scipy)

2.5 Mkm ↓  
• ♀ 3 spacecraft  
• At launch 2034  
• ~ 4yr mission

Sensitivity quoted as characteristic strain

$$S_n(f) = \frac{|\tilde{h}(f)|^2}{f_{\text{now}}} \leftarrow \begin{array}{l} \text{freq. domain} \\ \text{strain} \end{array}$$

$\sqrt{S_n(f)} \sqrt{\text{Hz}}$   
Measurement  
Bandwidth



of 100's resolvable

• Millions more stochastic (hopefully resolvable)

• Input from ~~GW~~ Gaia LSST, etc.

• "Verification binaries" seen with both GW & EM.

(~~GW~~ beneath which --)

Cosmological stochastic BS

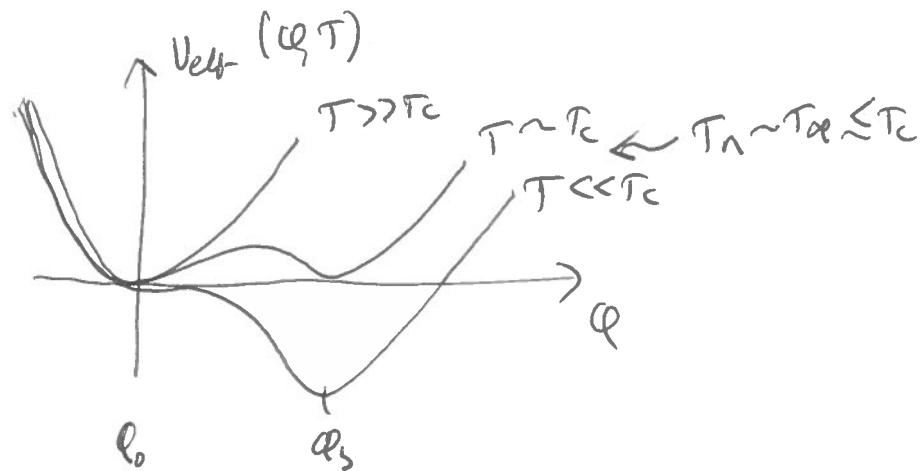
$\otimes = (\text{when } \text{GW}$   
made)

Hubble radius at  $T = T_\otimes \leftarrow$   
 $\sim \text{few cm} \xrightarrow[\text{today}]{\quad} \sim \text{few} \times 10^8 \text{ km}/$   
AU

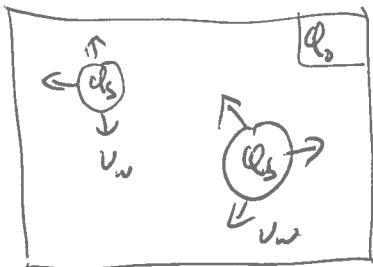
$[\otimes \approx \text{few} \times (\text{galactic binary radius})]$

⇒ important, but doable, to resolve / deal  
with binary background.

③ First-order phase transitions



→ Thermal transition: bubbles expand in SM plasma, and experience friction ( $v_w \lesssim c$ )



Rate/unit volume / unit time  
 $-S_3(T)/T$

$$\Gamma(T) = A(T) e^{-S_3(T)/T}$$

$\uparrow$   
 $\sim T^4$

Non-perturbative: hep-ph/0009132

④ The timescale (inverse) over which bubbles are made depends on how fast  $\Gamma(T)$  varies:

$$\frac{\beta}{H_d} = T_\alpha \left. \frac{dS}{dT} \right|_{T_\alpha}$$

Characteristic radius  $R_\alpha = (8\pi)^{1/3} \frac{V_\alpha}{\beta}$

Another important parameter is

$$\chi \equiv \chi_{T_\alpha}^{\alpha} = \frac{\Delta \phi(T)}{\epsilon_r(T)}$$

where  $\Delta \phi(T) = -\frac{T}{4} \frac{d}{dT} \Delta V + \Delta V$

$$\Delta V(T) = V_{eff}(\phi_0, T) - V_{eff}(\phi_s, T)$$

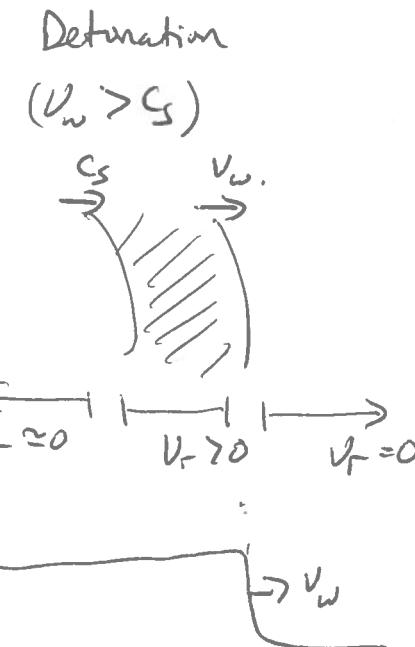
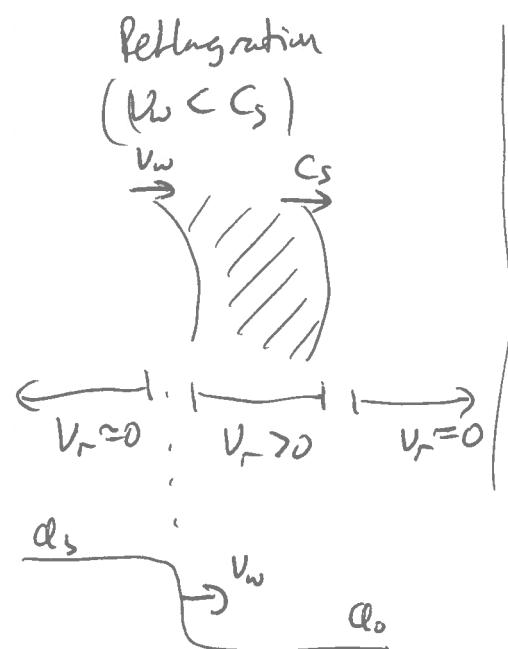
↓

$$\left\{ \chi, \frac{\beta}{H_d}, V_\alpha, T_\alpha, [g_d] \right\}$$

parameters  
that  
control non-  
eq<sup>n</sup> dynamics

Energy budget (1004.4187)

⑤ What do the reaction fronts look like?



Gravitational waves

$$\boxed{\exists h_{ij} = (16\pi G)(\tilde{\tau}_{ij}^h)^{TT} \in \text{transverse-traceless set}}$$

↑  
fluid stress-energy

$$\tilde{\tau}_{ij}^h = \omega u_i u_j$$

define  $\bar{u}_T^2 = \frac{1}{\omega V} \int_V d^3x \tilde{\tau}_{ii}^h$

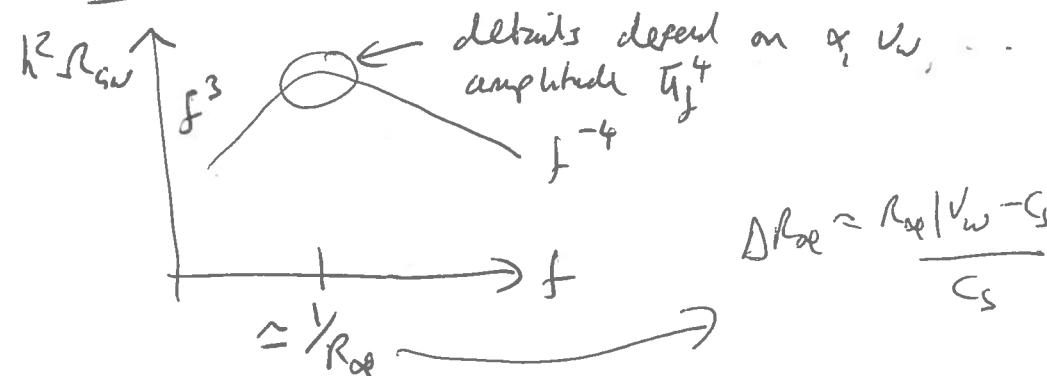
"enthalpy-weighted average velocity"

⑥ What sources GWs? shocks, turbulence, ...

When  $t \lesssim \min\{H_{\text{de}}^{-1}, R_{\text{de}}/U_r\}$ : sound (?)

Hubble damping

Sound: conservative option



But This is based on simulations with ~~assumptions~~  $\alpha \sim 10^{-3}$  (!)

[Optional: simulation details]  $\rightarrow \Theta$

$$(\partial_\mu \partial^\mu \varphi) \partial^\nu \varphi - \frac{\partial U_{\text{eff}}(\varphi, T)}{\partial \varphi} \partial^\nu \varphi$$

$$= \eta(\varphi, u_w, T) u^\mu \partial_\mu \varphi \partial^\nu \varphi$$

$$\begin{aligned} & \partial_\mu (\omega u^\mu u^\nu) - \partial^\nu \rho + \frac{\partial U_{\text{eff}}(\varphi, T)}{\partial \varphi} \partial^\nu \varphi \\ & = -\eta(\varphi, u_w, T) u^\mu \partial_\mu \varphi \partial^\nu \varphi \end{aligned}$$

⑦ What happens to the sound source  
when  $\alpha \sim 10^{-1}$ ?

→ Simulations of ideal fluid  $u^*$  ( $\approx$  SR plasma) coupled to scalar field  $\phi$  with friction term.

→ "Bag model" EoS, (not real eff. prof.).

⑧ Do nonlinearities / weird stuff appear?

1/ Retardation: ~~( $v_w > c_s$ )~~: no  
(at least not in the ~~initial~~  
immediate aftermath of the  
transition)

2/ Detlagations:  $(v_w < c_s)$ : yes!  
 → ~~fresh~~ Plasma reheats  
 → Walls slow down  
 → Kinematic ~~losses~~ efficiency  $\rightarrow 0$   
 (as  $\alpha \rightarrow \alpha_{\max}$ )

→ Less GWs than expected

→ Vorticity

